

# Inorganic Chemistry 1 – Chem. 2233

## Problem Set 3 (15 points)

Name: Answer key

ID #: \_\_\_\_\_

Please place final answers in the space provided for each question. There is no partial credit so make your final answer is clear.

The due date is: 9/27/2016

1 pt.  
each

1. State the coordination number of a sphere in each of the following arrangements:

(a) *ccp* 12, (b) *hcp* 12, (c) *bcc* 8, (d) *fcc* 12

1 pt.  
1 pt.

2. Beryllium has a hexagonal crystal structure, with  $a = 0.22858$  nm and  $c = 0.35842$  nm. The atomic radius is  $0.1143$  nm, the density is  $1.848$  g/cm<sup>3</sup>, and the atomic weight is  $9.01$  g/mol. Determine: *see p.2 for work*

a. The number of atoms in each unit cell: 2

b. The packing density (as a percentage) in the unit cell: 77%

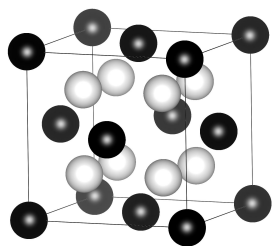
1 pt.

3. Nickel has the *fcc* crystal structure and a lattice parameter of  $a = 0.3517$  nm. Using this information, determine the atomic radius of Ni in angstroms: 1.243 Å *see p.2*

1 pt.

4. A compound is formed by two elements M and N. The element N forms *ccp* lattice and atoms of M occupy 1/3rd of the tetrahedral voids. What is the formula? M<sub>2</sub>N<sub>3</sub> *see p.2*

5. Given the following unit cell:



1 pt.  
1 pt.  
1 pt.

a. What is the composition of the unit cell? BA<sub>2</sub>

b. What is the most likely "Z value"? 4

c. What is the coordination environment of the "white" atoms? tetrahedral

$$\begin{aligned} \text{Black} = B &\rightarrow \left(\frac{1}{8} \times 8\right) + \left(\frac{1}{2} \times 6\right) = 4 \Rightarrow B_4A_8 = BA_2 \\ \text{White} = A &\rightarrow 8 \end{aligned}$$

*A are in Td holes of a fcc lattice of B, so there are 2 holes per atom of B.*

2 pt.

6. The equilibrium distance in diatomic LiF is  $1.52$  Å. Assuming ionic bonding between the two atoms, calculate the (lattice) energy required to separate them:  $Li^+ - F^- \rightarrow Li^+ + F^-$

answer:  $1.60 \times 10^3$  kJ/mol

2 pt.

7. Use the data given below to construct a Born-Haber cycle to determine the lattice energy of CaO following the reaction:  $Ca(s) + O_2 \rightarrow CaO$

Reaction	$\Delta H^\circ$ (kJ/mol)
Sub. of Ca	+193
IE1 of Ca	+590
IE2 of Ca	+1010
BDE of O <sub>2</sub>	+498
EA1 of O	-141
EA2 of O	+878
$\Delta H_f^\circ[CaO(s)]$	-635

answer:  $-3.41 \times 10^3$  kJ/mol

2. Volume of the hexagonal unit cell

$$V = (0.22858 \text{ nm})^2 (0.35842 \text{ nm}) \cos 30 = 0.01622 \text{ nm}^3 = 1.622 \times 10^{-23} \text{ cm}^3$$

(a) from the density equation

$$1.848 \frac{\text{g}}{\text{cm}^3} = \frac{(x \text{ atoms/cell})(9.01 \text{ g/mol})}{(1.622 \times 10^{-23} \text{ cm}^3)(6.022 \times 10^{23} \text{ atoms/mol})}$$

$$x = 2 \text{ atoms/cell}$$

(b) the packing density is

$$\text{PD} = \frac{(2 \text{ atoms/cell}) \left(\frac{4}{3} \pi\right) (0.1143 \text{ nm})^3}{0.01622 \text{ nm}^3} = 0.77$$

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3.  $r = \frac{a}{\sqrt{8}} = 0.124 \text{ nm}$  (see lecture 7)

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4. Count the  $N$  atoms in ccp lattice:  $\left(\frac{1}{8} \times 8\right) + \left(\frac{1}{2} \times 6\right) = 4$

$M$  atoms are in  $\frac{1}{3}$  of the tetrahedral holes. There are two tetrahedral holes per atom in the ccp lattice.

So  $4 \times 2 = 8$  tetrahedral holes

$$\text{and } 8 \times \frac{1}{3} = \frac{8}{3} M$$

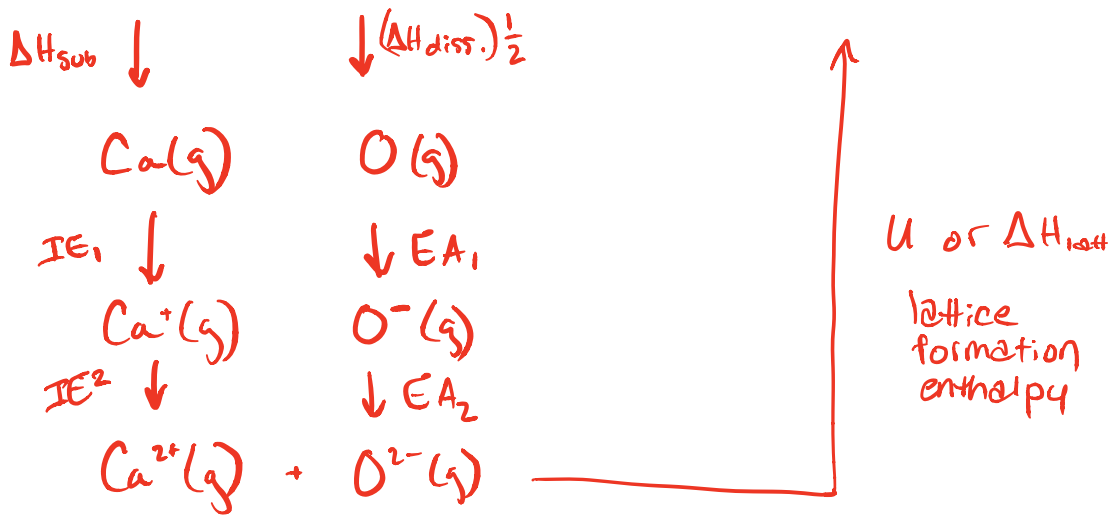
$$N:M = 4:\frac{8}{3} = 12:8 \rightarrow 3:2, M_2N_3$$

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6.  $r_{AB} = 1.52 \text{ \AA}$ ,  $A = 1.7476$  (NaCl-type structure)  $\epsilon_0 = 8.854 \times 10^{-12} \text{ Fm}^{-1} = \text{C}^2/\text{Jm}$

$$AU = -A \left( \frac{z_+ z_- e^2}{4\pi \epsilon_0 r_{AB}} \right) \rightarrow \text{(equation from lecture 8) for solids}$$

$$\begin{aligned}
&= -1.7476 \left( \frac{(1.602 \times 10^{-19} \text{ C})^2 \times 1 \times 1}{4\pi \cdot 8.854 \times 10^{-12} \text{ Fm}^{-1} \cdot 1.52 \times 10^{-10} \text{ m}} \right) \times \\
&\quad 6.022 \times 10^{23} \text{ mol}^{-1} \\
&= -1.597 \times 10^6 \text{ J/mol} \\
&= -1.60 \times 10^3 \text{ kJ/mol (lattice formation)} \\
&\quad \hookrightarrow +1.60 \times 10^3 \text{ kJ/mol (lattice separation)}
\end{aligned}$$



$$\Delta H_f^\circ = \Delta H_{\text{sub}} + \text{IE}_1 + \text{IE}_2 + \frac{1}{2} \Delta H_{\text{diss}} + \text{EA}_1 + \text{EA}_2 + U$$

$$U = \Delta H_f^\circ - \Delta H_{\text{sub}} - \text{IE}_1 - \text{IE}_2 - \Delta H_{\text{diss}} - \text{EA}_1 - \text{EA}_2$$

$$= -3.41 \times 10^3 \text{ kJ/mol}$$